

Name: _____

Date: _____

CW # 2-1: Math IB SL - Standard

17 - 21: Chapter 1 Review for Test

50 points

2 In an arithmetic sequence, $u_6 = -5$ and $u_9 = -20$. Find S_{20} .

$$u_n = d(n-1) + u_1$$

$$-5 = d(6-1) + u_1 \rightarrow (u_1 + 5d = -5) \rightarrow \begin{array}{r} -u_1 - 5d = 5 \\ + (u_1 + 8d = -20) \end{array}$$

Ans

$$-20 = d(9-1) + u_1$$

$$u_1 + 8d = -20$$

$$+ (u_1 + 8d = -20)$$

$$3d = -15$$

$$d = -5$$

$$-5 = 5(-5) + u_1$$

$$20 = u_1$$

$$S_{20} = \frac{20}{2} [-5(20-1) + 40]$$

$$S_{20} = -550$$

4 For the geometric series $0.5 - 0.1 + 0.02 \dots$
 $S_n = 0.416$. Find the number of terms in the series.

1	2	3	4	5
0.5	-0.1	0.02	-0.004	0.0008
0.5	0.4	0.42	0.416	

$$n = 4$$

7 How many terms are in the sequence 4, 7, 10, ..., 61?

$$d = 3 \quad u_1 = 4 \quad u_n = 61$$

$$\frac{61}{13}$$

$$61 = 3(n-1) + 4$$

$$57 = 3(n-1)$$

$$19 = n-1$$

$$n = 20$$

Name: _____

Date: _____

CW # 2-1: Math IB SL - Standard

17 - 21: Chapter 1 Review for Test

50 points

8 In a geometric sequence, the fourth term is 8 times the first term. If the sum of the first 8 terms is 765, find the 9th term of the sequence.

② $S_n = \frac{u_1(r^n - 1)}{r - 1}$
 $765 = \frac{u_1(2^8 - 1)}{2 - 1}$
 $765 = 255u_1$
 $u_1 = 3$

③ $u_9 = 3 \cdot 2^8$
 $u_9 = 768$

$u_4 = 8u_1, S_8 = 765$

① $u_n = u_1 \cdot r^{n-1}$
 $u_4 = u_1 \cdot r^3$
 $8u_1 = u_1 \cdot r^3$
 $\frac{8u_1}{u_1} = \frac{u_1 \cdot r^3}{u_1}$
 $8 = r^3$
 $2 = r$

9 Three consecutive terms of a geometric sequence are $x - 3$, 6 and $x + 2$. Find all possible values of x .

$r = \frac{6}{x-3}$ and $r = \frac{x+2}{6}$

$x = 7$ or $x = -6$

$\frac{6}{x-3} = \frac{x+2}{6}$

$(x-3)(x+2) = 36$
 $x^2 - 1x - 6 = 36$
 $x^2 - 1x - 42 = 0$
 $(x-7)(x+6) = 0$

14 Using the binomial theorem, expand $(3x - y)^6$.

$1(3x)^6(-y)^0 + 6(3x)^5(-y)^1 + 15(3x)^4(-y)^2 + 20(3x)^3(-y)^3$

$$\begin{array}{ccccccc} & & & & & & 1 \\ & & & & & 1 & \\ & & & & 1 & 2 & 1 \\ & & & 1 & 3 & 3 & 1 \\ & & 1 & 4 & 6 & 4 & 1 \\ & 1 & 5 & 10 & 10 & 5 & 1 \\ \hline 1 & 6 & 15 & 20 & 15 & 6 & 1 \end{array} n=6$$

$+ 15(3x)^2(-y)^4 + 6(3x)^1(-y)^5 + 1(3x)^0(-y)^6$

$729x^6 - 1458x^5y + 1215x^4y^2 - 540x^3y^3 + 135x^2y^4 - 18xy^5 + y^6$

22 P1: The 15th term of an arithmetic series is 143 and the 31st term is 183.

a Find the first term and the common difference.

(a) b Find the 100th term of the series.

$$\begin{aligned}
 143 &= d(15-1) + u_1 & \text{And} \\
 183 &= d(31-1) + u_1 & u_1 = -14(2.5) + 143 \\
 & & \boxed{u_1 = 108} \\
 \begin{array}{r}
 \downarrow \\
 30d + u_1 = 183 \\
 -(14d + u_1 = 143) \\
 \hline
 16d = 40 \Rightarrow \boxed{d = 2.5}
 \end{array}
 \end{aligned}$$

(b)

$$\begin{aligned}
 u_{100} &= 2.5(100-1) + 108 \\
 \boxed{u_{100} = 355.5}
 \end{aligned}$$

26 P1: The coefficient of x^2 in the binomial expansion of $(1+3x)^n$ is 495.

Determine the value of n .

$$\begin{aligned}
 \frac{n!}{2!(n-2)!} &= 55 \\
 \frac{n(n-1)(n-2)!}{2(n-2)!} &= \frac{55}{1}
 \end{aligned}$$

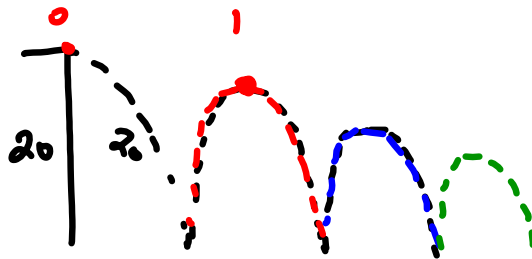
$$\begin{aligned}
 \binom{n}{r} a^{n-r} b^r & \quad (r=2) \\
 \binom{n}{2} (1)^{n-2} (3x)^2 & \\
 \frac{n!}{2!(n-2)!} [9x^2] & \quad \frac{495}{9} = 55
 \end{aligned}$$

$$n^2 - n = 110 \rightarrow n^2 - n - 110 = 0 \rightarrow (n-11)(n+10) = 0 \rightarrow \boxed{n=11} \quad n \neq -10$$

32 P1: A ball is dropped from a vertical height of 20m.

Following each bounce, it rebounds to a vertical height of $\frac{5}{6}$ its previous height.

Assuming that the ball continues to bounce indefinitely, show that the maximum distance it can travel is 220m.



$$20 + 2\left(\frac{5}{6}\right)(20) + 2\left(\frac{5}{6}\right)\left(\frac{5}{6}\right)(20) + 2\left(\frac{5}{6}\right)\left(\frac{5}{6}\right)\left(\frac{5}{6}\right)(20) + \dots$$

$$\left. \begin{aligned}
 u_1 &= 2\left(\frac{5}{6}\right)(20) \\
 u_1 &= \frac{200}{6} = \frac{100}{3}
 \end{aligned} \right\} S_{\infty} = \frac{\frac{100}{3}}{1 - \frac{5}{6}} = \left(\frac{100}{3}\right)\left(\frac{6}{1}\right) = \frac{600}{3} = 200$$

$$\text{Total} = 20 + 200 = \boxed{220}$$

(initial Height)