

Name: \_\_\_\_\_

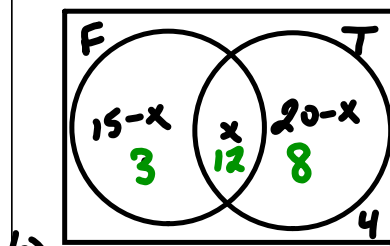
Show work needed to justify your answer.

Date: \_\_\_\_\_

HW: # 33a: Math IBSL - Standard 32 - Independent and Dependent Events and Conditional Probability 5 points

1 There are 27 students in a class. Of the students, 15 take film and 20 take theatre, and four do neither subject.

- a How many students take both subjects?
- b One person is chosen at random. Find the probability that the person:
  - i takes theatre but not film
  - ii takes at least one of the two subjects
  - iii takes theatre given that they take film.



(a)  $15-x+x+20-x+4=27$   
 $-x+39=27$   
 $x=12$

b(i)  $P(T \cap F') = \frac{8}{27}$

b(ii)  $P(T|F) = \frac{23}{27}$

b(iii)  $P(T|F) = \frac{P(T \cap F)}{P(F)}$   
 $= \frac{12}{15} = \frac{4}{5}$

2 A number is chosen at random from this list of eight numbers:

- 1 2 6 7 11 14 24 29

Find:

- a P(it is even | it is not a multiple of 4)
- b P(it is less than 15 | it is greater than 5)
- c P(It is less than 5 | it is less than 15) 3
- d P(it lies between 1 and 10 | it lies between 5 and 25)

a)  $P(E|N) = \frac{P(E \cap N^c)}{P(N^c)} = \frac{3}{7}$

b)  $P(L|G) = \frac{P(L \cap G)}{P(G)} = \frac{4}{6} = \frac{2}{3}$

c)  $P(L < 5 | L < 15) = \frac{P(L \cap \{5, 6, 7\})}{P(\{5, 6, 7\})} = \frac{2}{6} = \frac{1}{3}$

d)  $P(1-10 | 5-25) = \frac{P(A \cap B)}{P(B)} = \frac{3}{5}$

5 J and K are independent events. Given that  $P(J|K) = 0.3$  and  $P(K) = 0.5$ , find  $P(J)$ .

$P(J|K) = \frac{P(J \cap K)}{P(K)}$

$0.3 = \frac{P(J \cap K)}{0.5}$

$P(J \cap K) = 0.15$

$P(J \cap K) = P(J)P(K)$

$0.15 = 0.5 P(J)$

$P(J) = 0.3$

